

Diffraction of a Gaussian beam on a spiral axicon

V.V. Kotlyar¹, A.A. Kovalev², D. Kodzhek³, V. Garbini³, E. Ferrari^{1,3}

¹Image Processing Systems Institute of the RAS,

²Samara State Aerospace University (SSAU)

³Laboratory for Interdisciplinary Lithography, Trieste, Italy

Abstract

The study develops analytical relations that describe the Fresnel and Fraunhofer diffractions of a Gaussian beam on a spiral axicon (SA). The expressions are derived in the form of series of hypergeometric functions. The expression for the SA turns into the expression for a spiral phase plate (SPP) if the axicon parameter is set to zero. The functionality of such optical elements is verified both by numerical simulation and physical experiments using a spatial light modulator.

Keywords: Gaussian Beam, Axicon, spiral axicon, Fraunhofer diffraction, spiral phase plate.

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[Access full text \(in Russian\)](#)

References:

- [1] Khonina SN, Kotlyar VV, Soifer VA, Shinkaryev MV, Uspleniev GV. Trochoson. *Opt Commun* 1992; 91(3-4): 158-162. DOI: 10.1016/0030-4018(92)90430-Y.
- [2] Khonina SN, Kotlyar VV, Shinkarev MV, Soifer VA, Uspleniev GV. The phase rotor filter. *J Mod Opt* 1992; 39(5): 1147-1154. DOI: 10.1080/09500349214551151.
- [3] Fürhapter S, Jesacher A, Bernet S, Ritsch-Marte M. Spiral interferometry. *Opt Lett* 2006; 30(15): 1953-1955. DOI: 10.1364/OL.30.001953.
- [4] Bernet S, Jesacher A, Fürhapter S, Maurer C, Ritsch-Marte M. Quantitative imaging of complex samples by spiral phase contrast microscopy. *Opt Express* 2006; 14(9): 3792-3805. DOI: 10.1364/OE.14.003792.
- [5] Foo G, Palecios DM, Swartzlander GA. Optical vortex coronagraph. *Opt Lett* 2005; 30(24): 3308-3310. DOI: 10.1364/OL.30.003308.
- [6] Curtis JE, Grier DG. Structure of optical vortices. *Phys Rev Lett* 2003; 90(13): 133901. DOI: 10.1103/PhysRevLett.90.133901.
- [7] Lin J, Yuan X, Tao SH, Burge RE. Synthesis of multiple collinear helical modes generated by a phase-only element. *J Opt Soc Am A* 2006; 23(5): 1214-1218. DOI: 10.1364/JOSAA.23.001214.
- [8] Hakola A, Shevchenko A, Buchter SC, Kaivola M, Tabiryan NV. Creation of a narrow Bessel-like laser beam using a nematic liquid crystal. *J Opt Soc Am B* 2006; 23(4): 637-641. DOI: 10.1364/JOSAB.23.000637.
- [9] Chakraborty R, Ghosh A. Generation of an elliptic Bessel beam. *Opt Lett* 2006; 31(1): 38-40. DOI: 10.1364/OL.31.000038.
- [10] Bentley JB, Davis JA, Bandres MA, Gutiérrez-Vega JC. Generation of helical Ince-Gaussian beams with a liquid-crystal display. *Opt Lett* 2006; 31(5): 649-651. DOI: 10.1364/OL.31.000649.
- [11] Fatemi FK, Bashkansky M. Generation of hollow beams by using a binary spatial light modulator. *Opt Lett* 2006; 31(7): 864-866. DOI: 10.1364/OL.31.000864.
- [12] Whyte G, Courtial J. Experimental demonstration of holographic three-dimensional light shaping using a Gerchberg-Saxton algorithm. *New J Phys* 2005; 7(1): 117. DOI: 10.1088/1367-2630/7/1/117.
- [13] Wang Q, Sun XW, Shum P, Yin XJ. Dynamic switching of optical vortices with dynamic gamma-correction liquid-crystal spiral phase plate. *Opt Express* 2005; 13(25): 10285-10291. DOI: 10.1364/OPEX.13.010285.
- [14] Lin J, Yuan X, Tao SH, Peng X, Nin HB. Deterministic approach to the generation of modified helical beams for optical manipulation. *Opt Express* 2005; 13(10): 3862-3867.
- [15] Hahn J, Kim H, Choi K, Lee B. Real-time digital holographic beam-shaping system with a genetic feedback tuning loop. *Appl Opt* 2006; 45(5): 915-924. DOI: 10.1364/AO.45.000915.
- [16] Courtial J, Whyte G, Bouchel Z, Wagner J. Iterative algorithm for holographic shaping of non-diffracting and self-imaging light beams. *Opt Express* 2006; 14(6): 2108-2116. DOI: 10.1364/OE.14.002108.
- [17] Cojoc D, Di Fabrizio E, Businaro L, Carbini S, Romanato F, Vaccari L, Altissimo M. Design and fabrication of diffractive optical elements for optical tweezer arrays by means of e-beam lithography. *Microelectron Eng* 2002; 61-62: 963-969. DOI: 10.1016/S0167-9317(02)00426-4.
- [18] Kotlyar VV, Almazov AA, Khonina SN, Soifer VA, Elfstrom H, Turunen J. Generation of phase singularity through diffracting a plane or Gaussian beam by a spiral phase plate. *J Opt Soc Am A* 2005; 22(5): 849-861. DOI: 10.1364/JOSAA.22.000849.
- [19] Kotlyar VV, Khonina SN, Kovalev AA, Soifer VA, Elfstrom H, Turunen J. Diffraction of a plane, finite-radius wave by a spiral phase plate. *Opt Lett* 2006; 31(11): 1597-1599. DOI: 10.1364/OL.31.001597.
- [20] Kotlyar VV, Kovalev AA, Khonina SN, Skidanov RV, Soifer VA, Elfstrom H, Tossavainen N, Turunen J. Diffraction of conic and Gaussian beams by a spiral phase plate. *Appl Opt* 2006; 45(12): 2656-2665. DOI: 10.1364/AO.45.002656.
- [21] Ahluwalia BPS, Cheong WC, Yuan X-C, Zhang L-S, Tao S-H, Bu J, Wang H. Design and fabrication of a double-axicon for generation of tailorable self-imaged three-dimensional intensity voids. *Opt Lett* 2006; 31(7): 987-989. DOI: 10.1364/OL.31.000987.

- [22] Rozas D, Law CT, Swartzlander GA. Propagation dynamics of optical vortices. *J Opt Soc Am B* 1997; 14(11): 3054-3065. DOI: 10.1364/JOSAB.14.003054.
- [23] Dennis MR. Rows of optical vortices from elliptically perturbing a high-order beam. *Opt Lett* 2006; 31(9): 1325-1327. DOI: 10.1364/OL.31.001325.
- [24] Swartzlander GA. Broadband nulling of a vortex phase mask. *Opt Lett* 2005; 30(21): 2876-2878. DOI: 10.1364/OL.30.002876.
- [25] Cheong WC, Lee W, Yuan X-C, Zhang L-S, Dholakia K, Wang H. Direct electron-beam writing of continuous spiral phase plates in negative resist with high power efficiency for optical manipulation. *Appl Phys Lett* 2004; 85(23): 5784-5786. DOI: 10.1063/1.1830678.
- [26] Polin M, Ladavac K, Lee S, Roichman Y, Gviev DG. Optimized holographic optical traps. *Opt Express* 2005; 13(15): 5831-5845. DOI: 10.1364/OPEX.13.005831.
- [27] Prudnikov AP, Brichkov YA, Marichev OI. Integrals and series. Volume 2: Special functions. CRC Press; 1986. ISBN: 978-2-88124-090-4.